

Contact Mechanics and Elements of Tribology

Lecture 4.

Contact and Mechanics of Materials

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@ Centre des Matériaux
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Surface/near-surface properties

Surface properties:

- Friction
- Adhesion
- Wear

Surface/near-surface properties

Surface properties **are not fundamental**

- Friction 😞
- Adhesion 😞
- Wear 😞

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- Friction ☹️
- Adhesion ☹️
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Fundamental properties:

■ **Volume:**

- Young's modulus
- Poisson's ratio
- shear modulus
- yield stress
- mass density
- thermal properties

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■ Surface:

- chemical reactivity
- absorption capabilities
- surface energy
- roughness

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Fundamental properties **are interdependent**

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Surface/near-surface properties

Surface properties **are not fundamental**

- Friction ☹️
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More fundamental properties

- solids are made of atoms
- atoms are linked by bonds
- most of the **volume** and **surface** properties are the **properties of the bonds**

Fundamental properties **are interdependent**

■ Volume:

- Young's modulus
- Poisson's ratio
- shear modulus
- yield stress
- mass density
- thermal properties

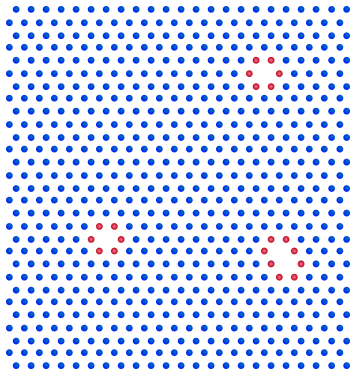
■ Surface:

- chemical reactivity
- absorption capabilities
- surface energy
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Let's use atoms to simulate contacts

Let's start from the bottom

- Use Molecular Dynamics
- Potential for interaction between particles
- Time integration of the system evolution
- Natural coupling between thermal and mechanical phenomena
- Inherent plasticity (dislocation movement)

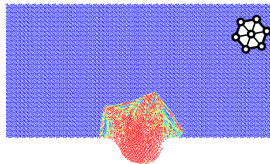
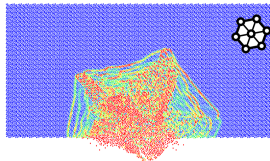
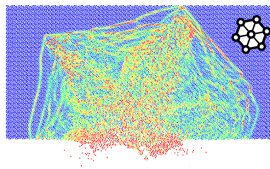


Example: high-velocity impact

Impact of a perfect crystal by a circular projectile

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Example: high-velocity impact

Impact of a perfect crystal by a circular projectile: 20 000 particles on 20 000 time steps.

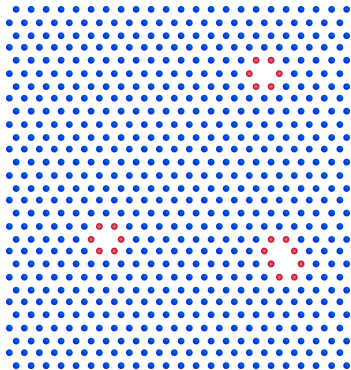
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Unfortunately it is hard to obtain valuable results at macroscopic scale using MD ...

- How to get rid of the inherent adhesion between two surfaces?
- Hard to scale roughness to representative scale
- Too huge 3D simulations even for nano-indentation

Onset of plastic yielding

Hertz contact: body of revolution

- Onset of plasticity for pressure

$$p_Y = 1.6\sigma_Y$$

- Associated force

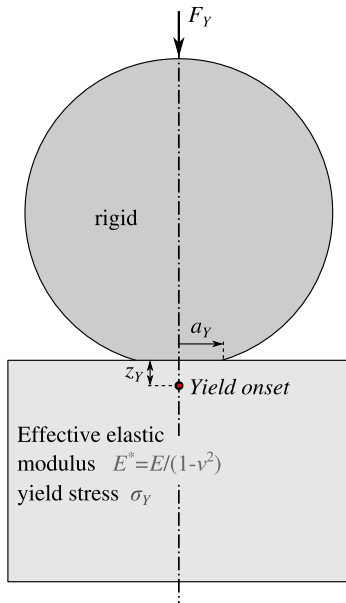
$$F_Y = \frac{1.6^3\pi^3R^2}{6} \left(\frac{\sigma_Y}{E^*}\right)^2 \sigma_Y$$

- Associated contact radius

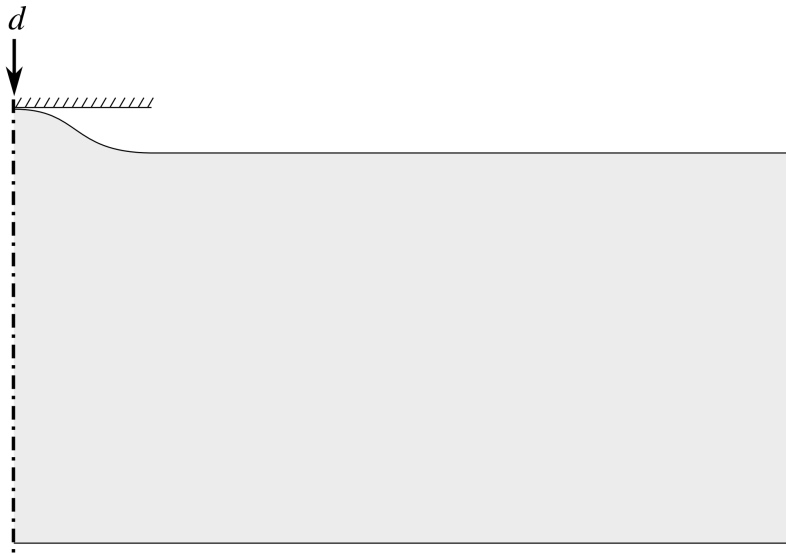
$$a_Y = \frac{1.6\pi R}{2} \frac{\sigma_Y}{E^*}$$

- Plastic flow starts at depth

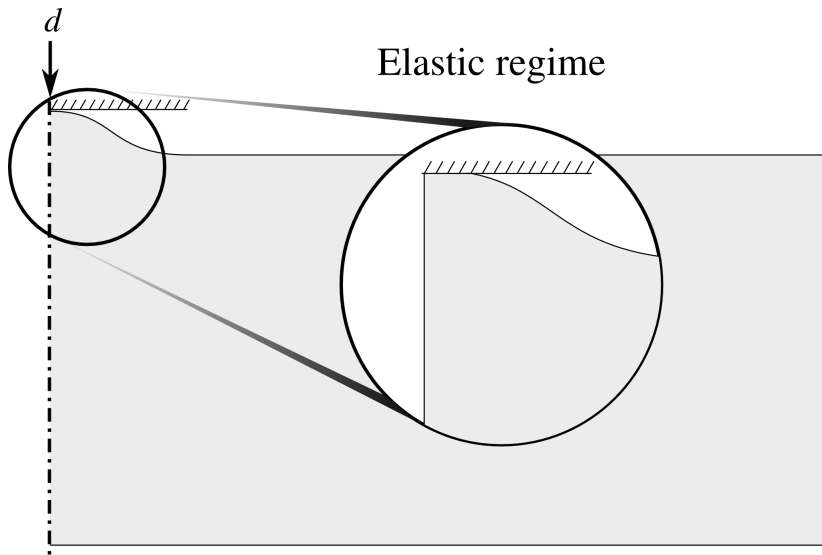
$$z_Y \approx 1.21R \frac{\sigma_Y}{E^*}$$



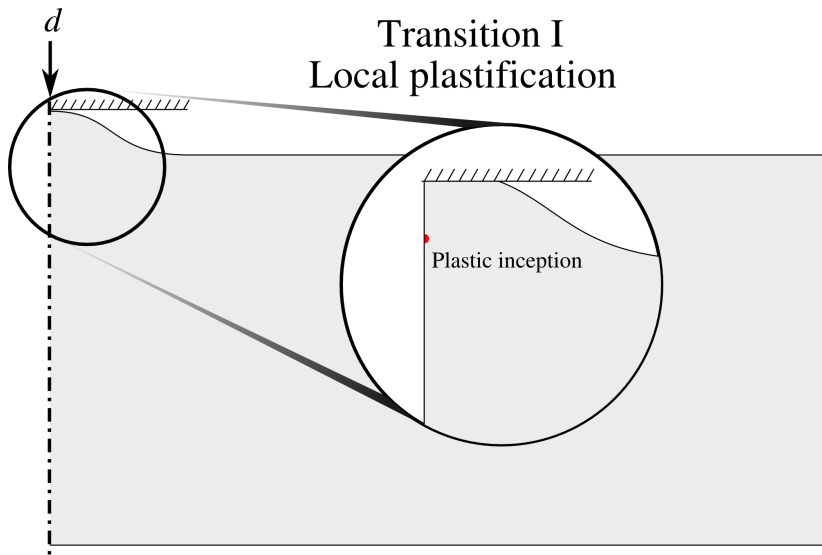
Elasto-plastic transition in contact



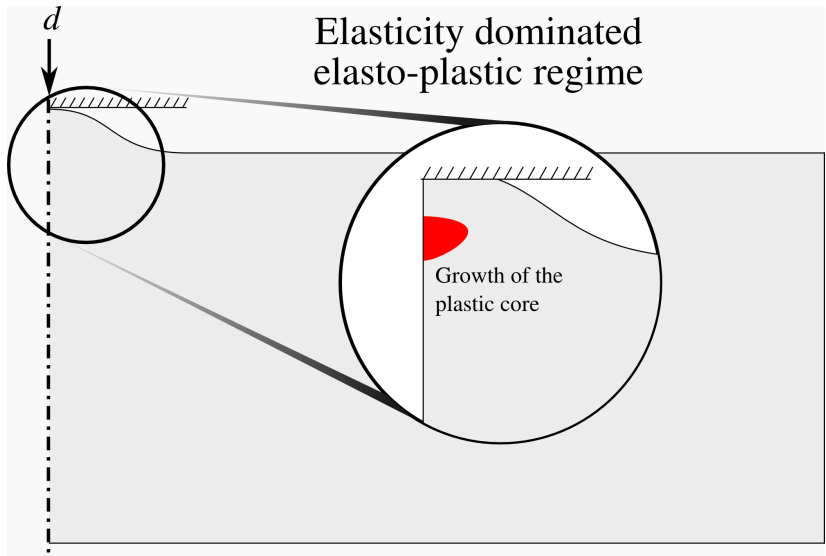
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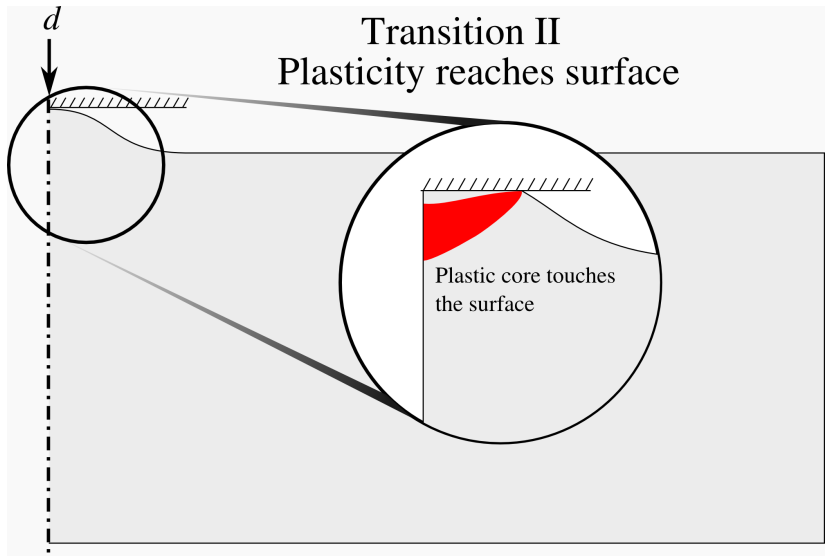
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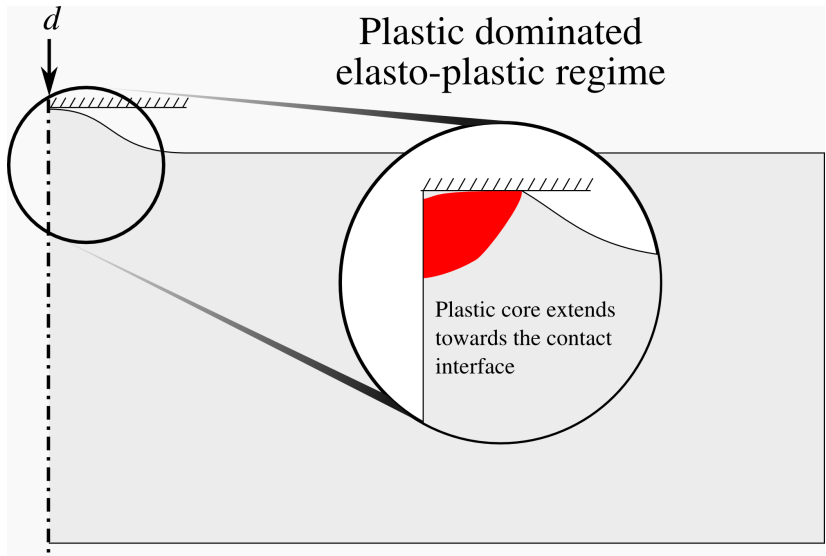
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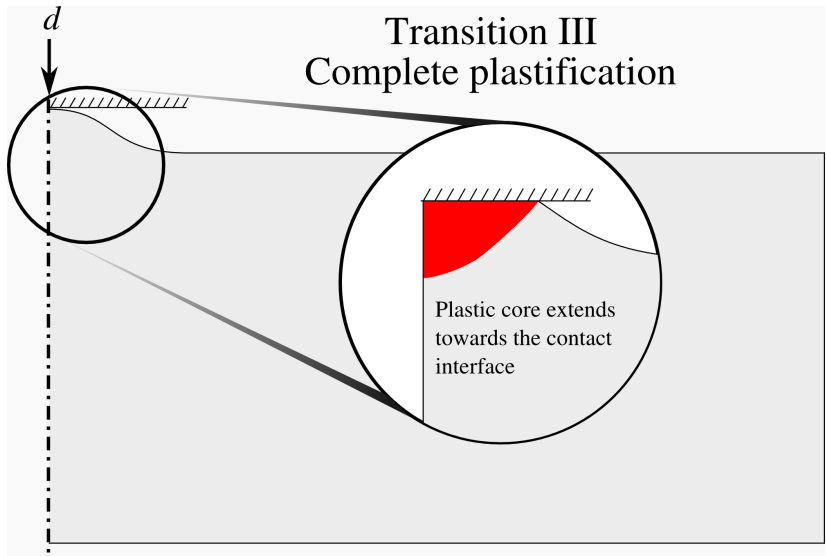
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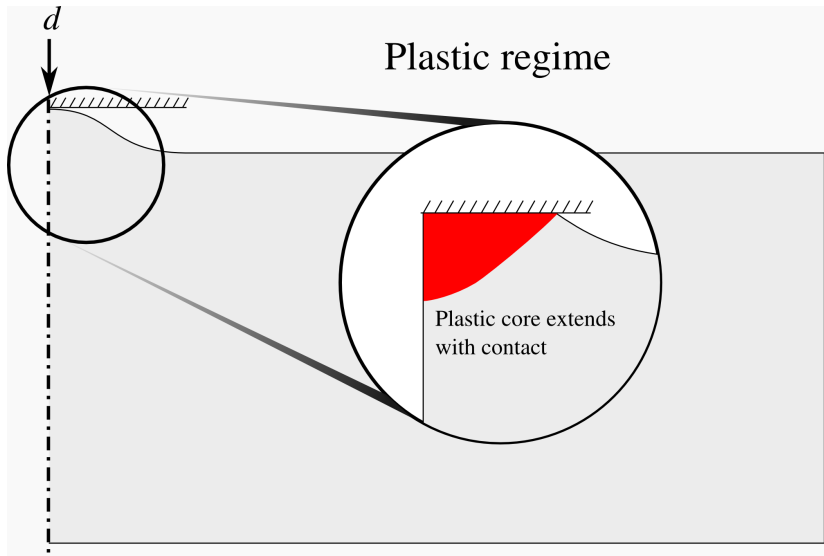
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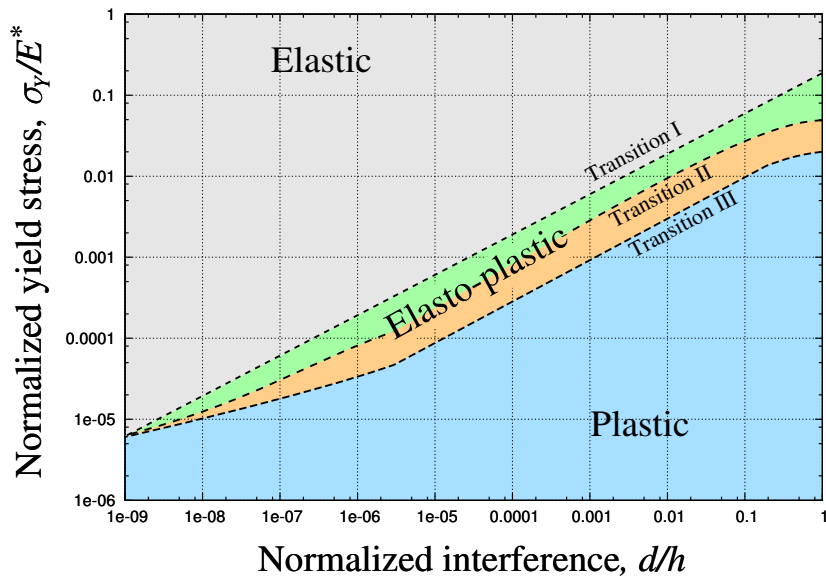
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Elasto-plastic transition in contact

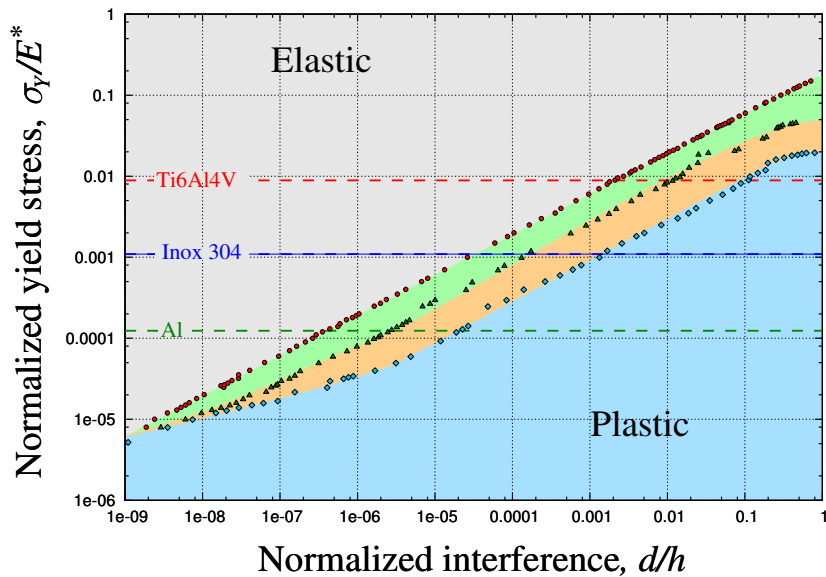


Elasto-plastic transition in contact



Deformation map for a sinusoidal asperity constructed with Ming Liu

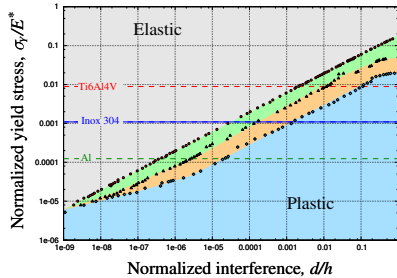
Elasto-plastic transition in contact



Deformation map for a sinusoidal asperity constructed with Ming Liu

Elasto-plastic transition in contact

Case: $\sigma_Y/E = 0.0005$



Evolution of the plastic zone in a sinusoidal asperity in contact with a rigid flat

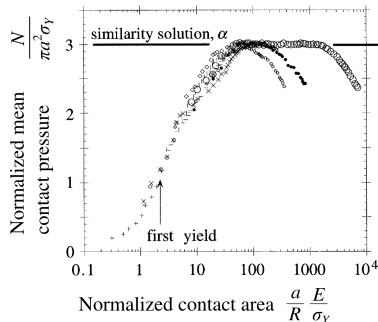
Elastic-plastic normal contact: hardness

- Hardness $\sim$ saturated plastic contact
- Recall: Vickers hardness
 $HV = N/A$
- Similarity solution^[1]

$$\frac{N}{\pi a^2 \sigma_Y} = F \left(\frac{a}{R} \frac{E}{\sigma_Y} \right)$$

- Hardness $H \approx 3\sigma_Y$

[1] Hill R., Storåkers B., Zdunek A.B. A theoretical study of the Brinell hardness test. Proc R Soc Lond A 436 (1989)



Simulation of spherical indentation of elasto-plastic solid with power-law hardening^[2]

Mesarovic S., N. Fleck, Spherical Indentation of Elastic-Plastic Solids, Proc R Soc Lond A 455 (1999)

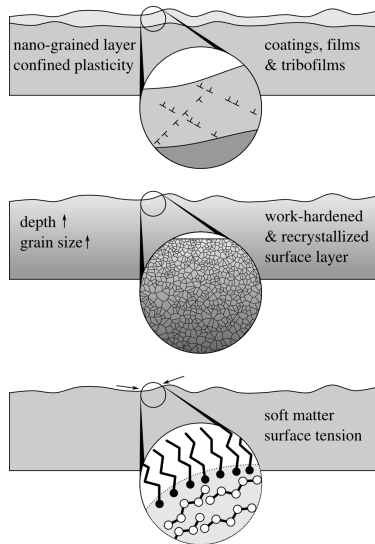
Near-surface vs bulk deformation

Material aspects

- Cold worked surface + recrystallized:
smaller grains near the surface,
Hall-Petch effect
- Thin coating films:
nanograined, confined plasticity,
Hall-Petch effect
- Oxides:
brittle hard films

Geometrical aspects

- Roughness of all nature
- Indentation by asperities:
confined plastic zone, high plastic
strain gradients



Onset of yielding at atomic scale

Hertz contact: body of revolution

- Onset of plasticity for pressure

$$p_Y = 1.6\sigma_Y$$

- Associated force

$$F_Y = \frac{1.6^3 \pi^3 R^2}{6} \left(\frac{\sigma_Y}{E^*} \right)^2 \sigma_Y$$

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- Plastic flow starts at depth

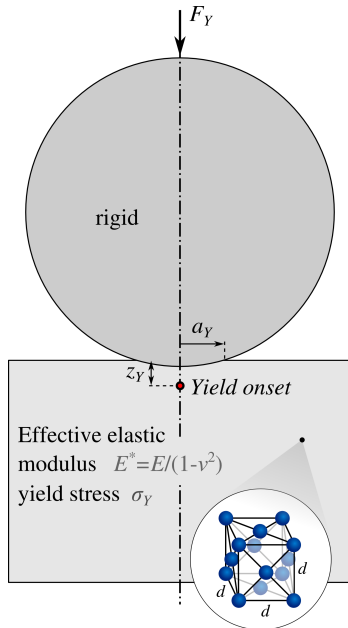
$$z_Y \approx 1.21R \frac{\sigma_Y}{E^*}$$

- Example: golden asperity $R = 10 \mu\text{m}$

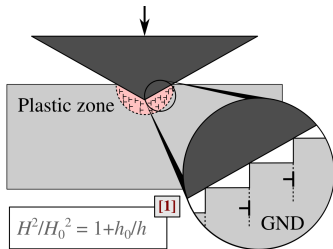
$$E^* \approx 96 \text{ GPa}, \quad \sigma_Y \approx 140 \text{ MPa}, \quad d \approx 4.1 \text{ \AA}$$

$$F_Y \approx 3.8 \mu\text{N}, \quad z_Y \approx 18 \text{ nm}, \quad a_Y \approx 36 \text{ nm}$$

$$z_Y \approx 45d, \quad a_Y \approx 115d$$

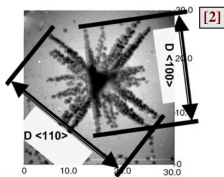
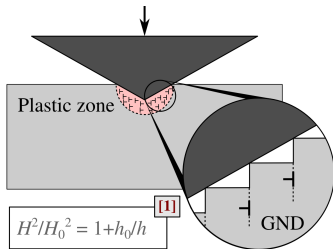


Indentation and hardness



[1] Nix, Gao. *J Mech Phys Solids* (1998).

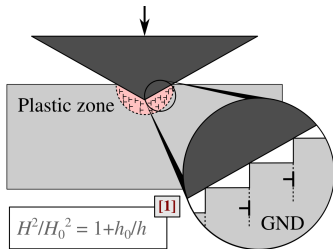
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[1] Nix, Gao. *J Mech Phys Solids* (1998).

[2] Feng, Nix. *Scripta Mater* (2004).

Indentation and hardness



$$H^2/H_0^2 = 1 + h_0/h$$

$$\frac{\text{Plastic zone } r}{\text{Contact radius } a} \sim 1 + b \exp(-h/h_1)$$

$$H^2/H_0^2 = 1 + [1 + b \exp(-h/h_1)]^{-3} h_0/h$$

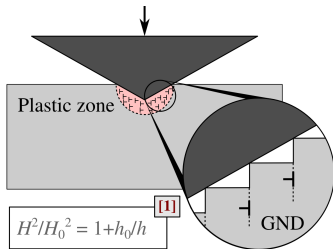
$$(H - H_p)^2 / (H_0 - H_p)^2 = 1 + [1 + b \exp(-h/h_1)]^{-3} h_0/h$$

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[2] Feng, Nix. *Scripta Mater* (2004).

[3] Qui, Huang, Nix, Hwang, Gao. *Acta Mater* (2001).

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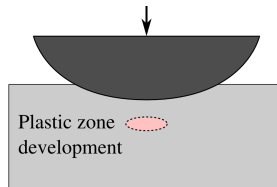
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[2]

$$(H - H_p)^2 / (H_0 - H_p)^2 = 1 + [1 + b \exp(-h/h_1)]^{-3} h_0/h$$

[2,3]

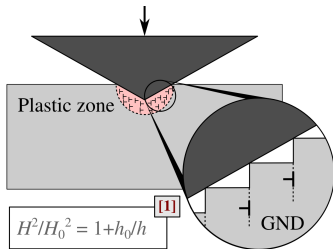


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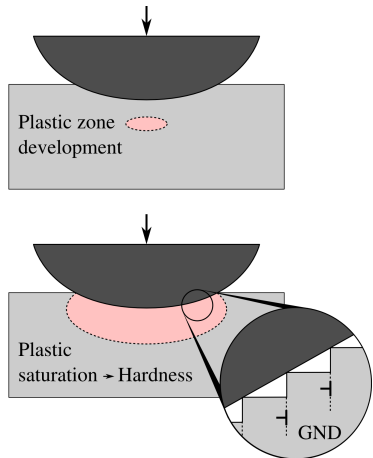
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This equation is associated with reference [2].

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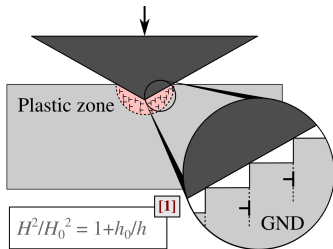


[1] Nix, Gao. *J Mech Phys Solids* (1998).

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Indentation and hardness



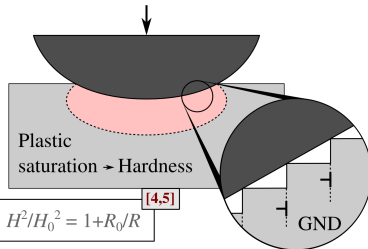
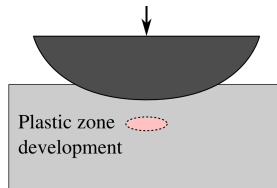
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[4] Swadener, George, Pharr. *J Mech Phys Solids* (2002).

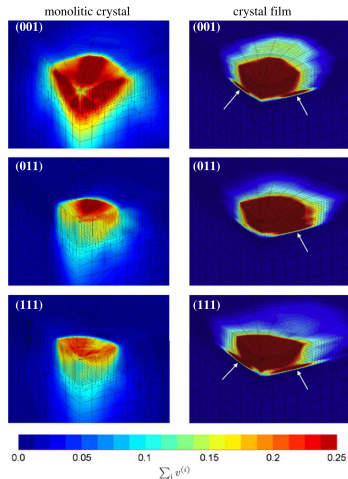
[5] Gao, Larson, Lee, Nicola, Tischler, Pharr. *J Appl Mech* (2015).

Enhanced material behavior: beyond J2 plasticity

- Crystal plasticity models
in indentation all slip systems are activated
Difference with isotropic plasticity is small
- Discrete models with inherent characteristic length
 - Molecular Dynamics
 - Dislocation Dynamics
- Continuum models with characteristic length
 - Cosserat continuum^[1]
 - Second-gradient plasticity^[2]

[1] Forest S., Sievert R. Elastoviscoplastic constitutive frameworks for generalized continua. Acta Mech 160 (2003)

[2] Cordero N.M., Forest S. et al. Grain size effects on plastic strain and dislocation density tensor fields in metal polycrystals, Comp Mater Sci 52 (2012)

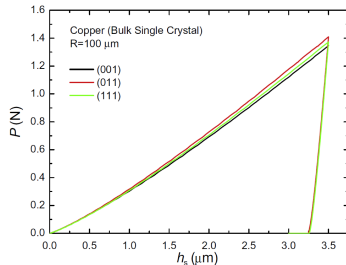


Spherical indentation of FCC copper crystal using crystal plasticity model in Zset

Casals O., Forest S. Finite element crystal plasticity analysis of spherical indentation in bulk single crystals and coatings. Comp Mater Sci 45 (2009)

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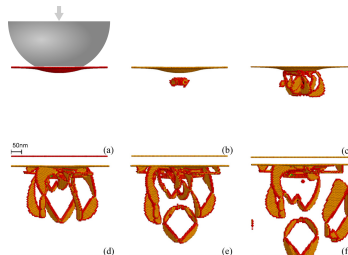
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MD simulation of a spherical indentation on (111) FCC cube

[1] H.J. Chang, M. Fivel, D. Rodney, M. Verdier.
Multiscale modelling of indentation in FCC
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11 (2010)

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Resulting DD simulation of a spherical indentation on (111) FCC cube

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www.numodis.com

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DD simulation of Berkovich nanoindentation

www.numodis.com

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Cosserat continuum

- Field variables (displacement & rotation): $\underline{u}, \underline{\omega}$
- Small deformation tensor: $\underline{\underline{\epsilon}} = \nabla \underline{u} + {}^3\underline{\underline{\epsilon}} \cdot \underline{\omega}$
- Torsion-curvature tensor: $\underline{\underline{\kappa}} = \nabla \underline{\omega}$
- Elasticity: $\underline{\underline{\sigma}} = \lambda \text{tr} \left(\underline{\underline{\epsilon}} \right) \underline{\underline{I}} + \mu (\underline{\underline{\epsilon}} + \underline{\underline{\epsilon}}^\top) + \mu_c (\underline{\underline{\epsilon}} - \underline{\underline{\epsilon}}^\top), \quad \underline{\underline{m}} = \alpha \text{tr} \left(\underline{\underline{\kappa}} \right) \underline{\underline{I}} + 2\beta \underline{\underline{\kappa}}$

$$l_e = \sqrt{\beta/\mu}$$

Note: $\underline{\underline{\epsilon}}^\top \neq \underline{\underline{\epsilon}}, \underline{\underline{\kappa}}^\top \neq \underline{\underline{\kappa}}, \underline{\underline{\sigma}}^\top \neq \underline{\underline{\sigma}}, \underline{\underline{m}}^\top \neq \underline{\underline{m}}$

- In non-inertial problems without volume forces and couple-forces, balance of momentum and of moment of momentum:

$$\nabla \cdot \underline{\underline{\sigma}} = 0, \quad \nabla \cdot \underline{\underline{m}} - {}^3\underline{\underline{\epsilon}} : \underline{\underline{\sigma}} = 0$$

- Plasticity: equivalent stress^[1,2] $\Upsilon = \sqrt{\frac{3}{2} \left(a_1 \underline{\underline{s}} : \underline{\underline{s}} + a_2 \underline{\underline{s}} : \underline{\underline{s}}^\top + \left[\frac{1}{l_p^2} \right] \underline{\underline{m}} : \underline{\underline{m}} \right)}$
- Internal lengths: elastic l_e , plastic l_p

[1] R. de Borst, L.J. Sluys, *Comp Meth Appl Mech Engin* (1991)

[2] S. Forest, R. Sievert, *Acta Mech* (2003)

$$\text{where permutation tensor } {}^3\underline{\underline{\epsilon}} \sim \epsilon_{ijk} = \begin{cases} 1, & \text{if } \{ijk\} = \{123\} \text{ or } \{231\} \text{ or } \{312\} \\ -1, & \text{if } \{ijk\} = \{321\} \text{ or } \{213\} \text{ or } \{132\} \\ 0, & \text{otherwise} \end{cases}$$

Single asperity analysis

Assumptions

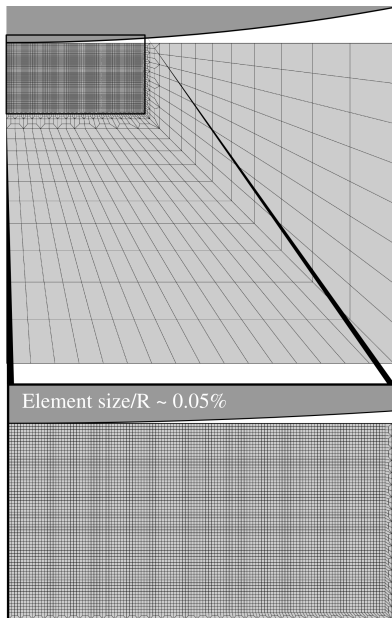
- Rigid spherical asperity
- Axisymmetric FE problem
- Generalized Cosserat continuum

Parameters

- Au: $E = 96 \text{ GPa}$, $\nu = 0.42$,
 $\sigma_y = 140 \text{ MPa}$
- $\mu_c = 10\mu$, $l_e = 100 \text{ nm}$, $a_1 = 1$
- Indenter radius
 $R \in [0.002, 2000] \mu\text{m}$

Objectives

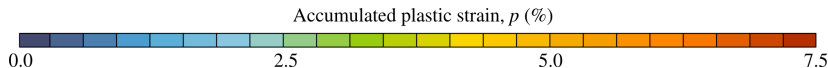
- Study size effect
- Enhance asperity based models
for rough contact



Element size/ $R \sim 0.05\%$

Accumulated plasticity

- Different plastic distribution



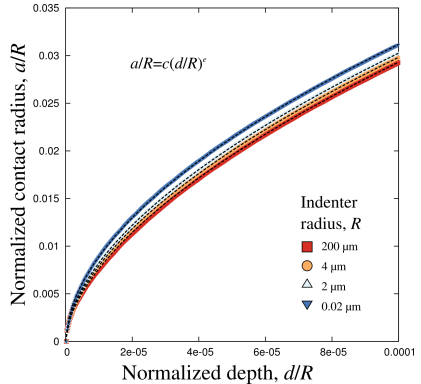
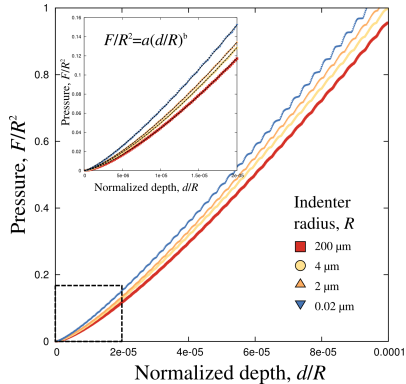
Displacement $\times 5$

Indenter radius $R = 20\mu\text{m}$
Max plastic strain $p_{\text{max}} \approx 7.5\%$

Displacement $\times 5$

Indenter radius $R = 2\mu\text{m}$
Max plastic strain $p_{\text{max}} \approx 11\%$

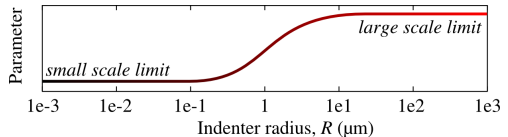
Displacement–force–contact radius



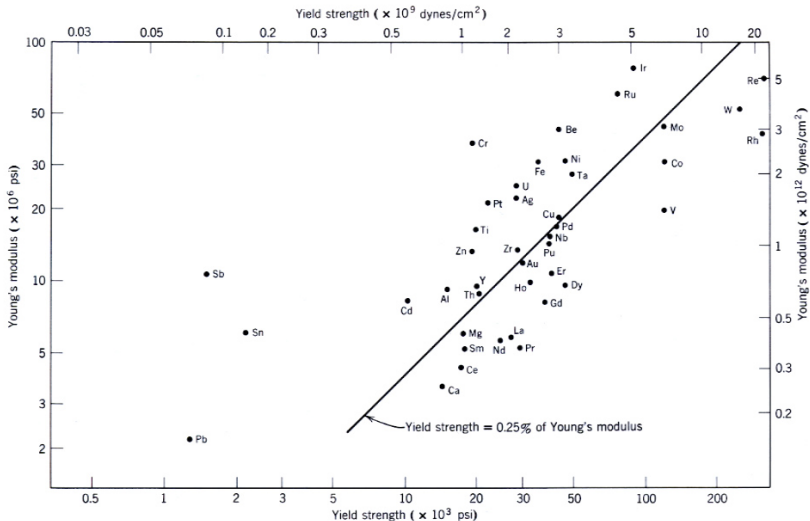
Parameters:

$a(R), b(R), c(R), e(R)$

else: using NURBS curve fit.



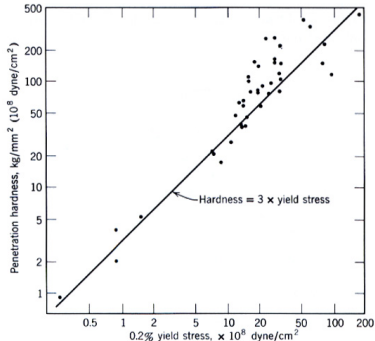
Material properties interdependence



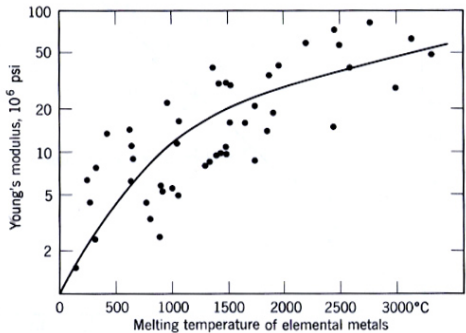
Young's modulus and yield strength interdependence

Rabinowicz, Friction and wear of materials, Wiley (1965)

Material properties interdependence



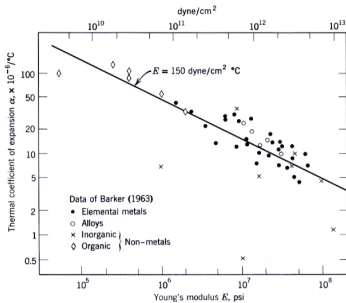
Penetration hardness and yield stress interdependence



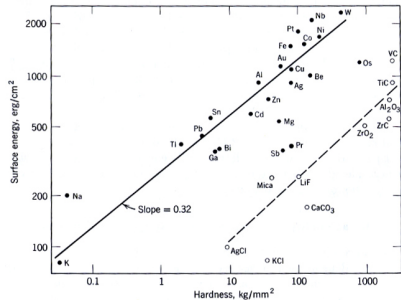
Young's modulus and melting temperature interdependence

Rabinowicz, Friction and wear of materials, Wiley (1965)

Material properties interdependence



Thermal coefficient of expansion and Young's modulus interdependence



Surface energy and hardness interdependence

Rabinowicz, Friction and wear of materials, Wiley (1965)

Real area of contact

Real area of contact depends on

Real area of contact

Real area of contact depends on

- **normal load:**

real area of contact is proportional to the normal load and inversely proportional to the hardness H

$$A_r \sim p_0$$

A_r - real contact area, p_0 - applied pressure

Real area of contact

Real area of contact depends on

- **normal load:**

real area of contact is proportional to the normal load and inversely proportional to the hardness H

$$A_r = A_0 \frac{p_0}{H}$$

A_r - real contact area, p_0 - applied pressure; H - hardness, A_0 - nominal contact area

Real area of contact

Real area of contact depends on

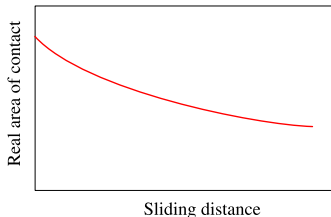
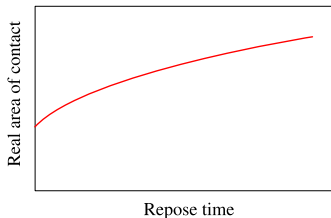
■ normal load:

real area of contact is proportional to the normal load and inversely proportional to the hardness H

■ sliding distance:

contact area might be significantly smaller than before shear forces were first applied

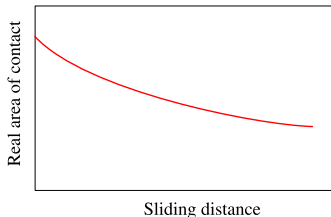
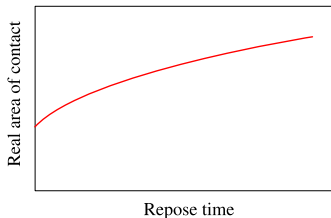
$$A_r = A_0 \frac{p_0}{H}$$



Real area of contact depends on

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contact area might be significantly smaller than before shear forces were first applied
- **time:**
real area of contact increases with time
(for *creeping materials*)

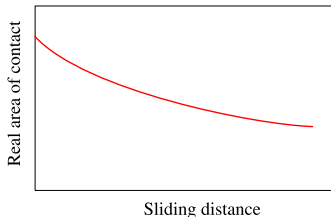
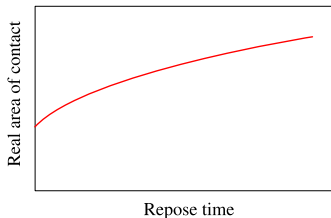
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- **sliding distance:**
contact area might be significantly smaller than before shear forces were first applied
- **time:**
real area of contact increases with time (*for creeping materials*)
- **surface energy:**
the higher the surface energy, the greater the area of contact

$$A_r = A_0 \frac{p_0}{H}$$



First approximations: friction coefficient does not depend on

- normal load
 - apparent area of contact
 - velocity
 - sliding surface roughness
 - time
-
- Friction force direction is opposite to the sliding

First approximations: friction coefficient does not depend on

- normal load 😊/😞
 - apparent area of contact 😊
 - velocity 😞
 - sliding surface roughness 😞/😊
 - time 😞/😊
-
- Friction force direction is opposite to the sliding 😊

Real friction :: normal load

First approximation:

- friction coefficient
does not depend on
normal load.

Exceptions:

Real friction :: normal load

First approximation:

- friction coefficient does not depend on normal load.

Exceptions:

- at micro scale for small slidings

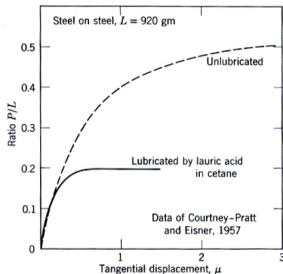


Fig. 1. For very small sliding, the force of friction is not proportional to the normal force^[1]

[1] Rabinowicz, Friction and wear of materials, Wiley (1965)

Real friction :: normal load

First approximation:

- friction coefficient does not depend on normal load.

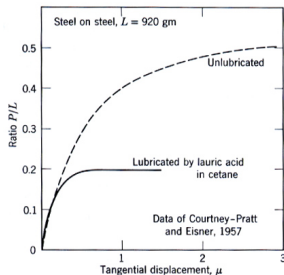


Fig. 1. For very small sliding, the force of friction is not proportional to the normal force^[1]

Exceptions:

- at micro scale for small slidings
- for huge pressures (metal forming) friction force is limited

[1] Rabinowicz, Friction and wear of materials, Wiley (1965)

Real friction :: normal load

First approximation:

- friction coefficient does not depend on normal load.

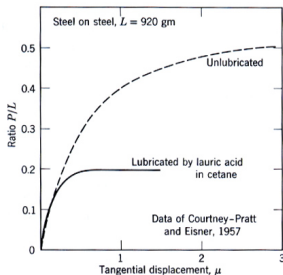


Fig. 1. For very small sliding, the force of friction is not proportional to the normal force^[1]

Exceptions:

- at micro scale for small slidings
- for huge pressures (metal forming) friction force is limited
- for too hard (diamond) or too soft (teflon) materials:
 - generally $T = cF^\alpha$, $\alpha \in \left[\frac{2}{3}; 1\right]$;

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Real friction :: normal load

First approximation:

- friction coefficient does not depend on normal load.

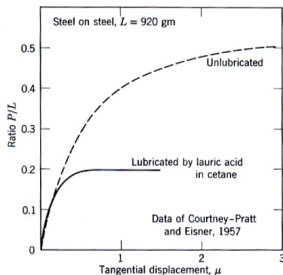


Fig. 1. For very small sliding, the force of friction is not proportional to the normal force^[1]

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Exceptions:

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- for huge pressures (metal forming) friction force is limited
- for too hard (diamond) or too soft (teflon) materials:
 - generally $T = cF^\alpha$, $\alpha \in [\frac{2}{3}; 1]$;
- hard coating (film) and a softer substrate

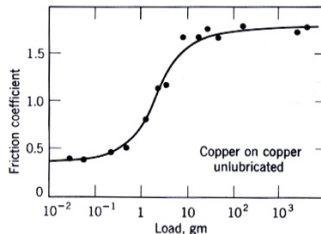
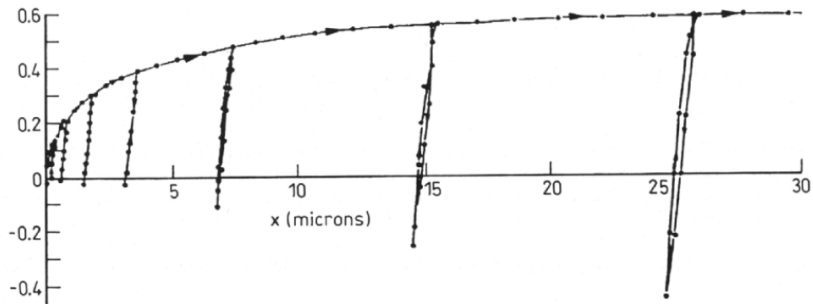


Fig. 2. Hard film on a softer substrate, at moderate loads friction is determined by the film friction, at higher loads, the coating brakes and softer material determines the frictional properties^[1]

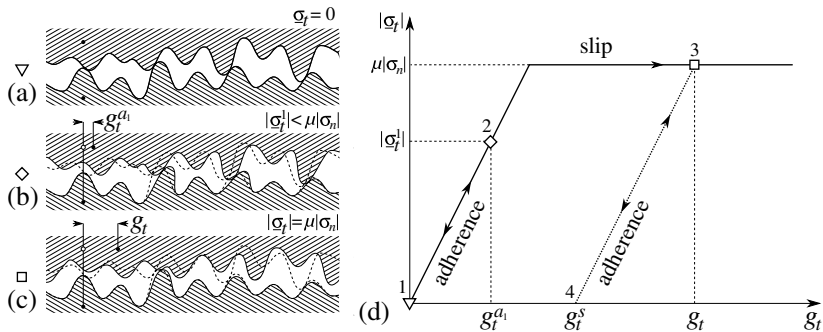
Real friction :: normal force



Friction coefficient versus tangential movement

Courtney-Pratt J. S., and E. Eisner. The effect of a tangential force on the contact of metallic bodies. Proc R Soc A 238 (1957)

Real friction :: normal force



Asperity deformations in the contact interface



First approximation:

- friction force
direction is opposite
to the sliding.

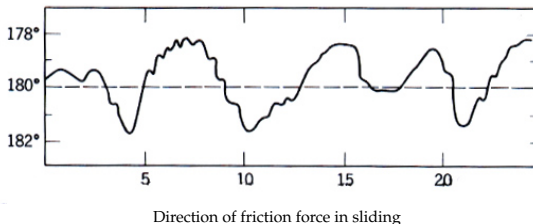
Real friction :: friction direction

First approximation:

- friction force direction is opposite to the sliding.

Exceptions:

- the direction of the friction force remains within $[178; 182]$ degrees to sliding direction (fig. 1);



[1] Rabinowicz, Friction and wear of materials, Wiley (1965)

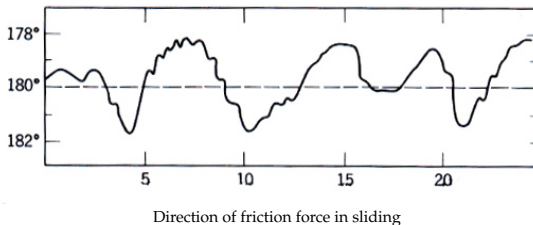
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Exceptions:

- the direction of the friction force remains within $[178; 182]$ degrees to sliding direction (fig. 1);
- the difference is higher for anisotropic surface roughness



[1] Rabinowicz, Friction and wear of materials, Wiley (1965)

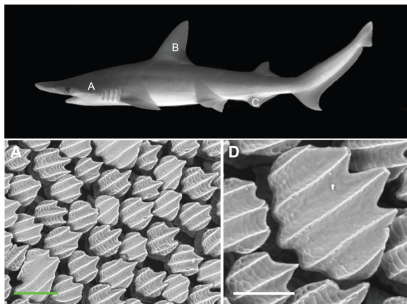
Real friction :: friction direction

First approximation:

- friction force direction is opposite to the sliding.

Exceptions:

- the direction of the friction force remains within $[178; 182]$ degrees to sliding direction (fig. 1);
- the difference is higher for anisotropic surface roughness
- asymmetry of roughness and friction



Examples of asymmetric friction

Real friction :: apparent area and roughness

First approximation:

- Friction coefficient does not depend on the apparent area of contact

Exceptions:

First approximation:

- Friction coefficient does not depend on surface roughness

Exceptions:

Real friction :: apparent area and roughness

First approximation:

- Friction coefficient does not depend on the apparent area of contact

Exceptions:

- very smooth and clean surfaces

First approximation:

- Friction coefficient does not depend on surface roughness

Exceptions:

Real friction :: apparent area and roughness

First approximation:

- Friction coefficient does not depend on the apparent area of contact

Exceptions:

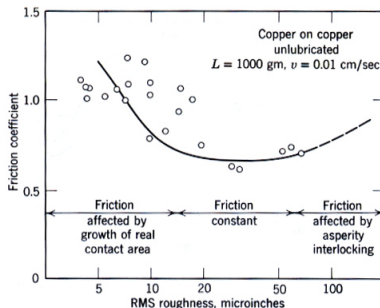
- very smooth and clean surfaces

First approximation:

- Friction coefficient does not depend on surface roughness

Exceptions:

- too smooth or too rough surfaces



Effect of roughness on the coefficient of friction

[1] Rabinowicz, Friction and wear of materials, Wiley (1965)

Real friction :: time and velocity

First approximation:

- Friction coefficient does not depend on time

Exceptions:

First approximation:

- Friction coefficient does not depend on sliding velocity

Exceptions:

Real friction :: time and velocity

First approximation:

- Friction coefficient does not depend on time

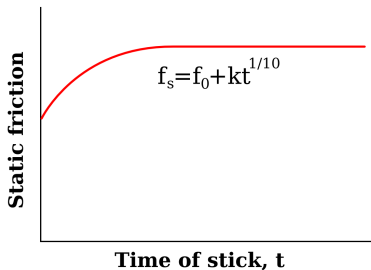
Exceptions:

- creeping materials

First approximation:

- Friction coefficient does not depend on sliding velocity

Exceptions:



Evolution of the static coefficient of friction with the time of repose

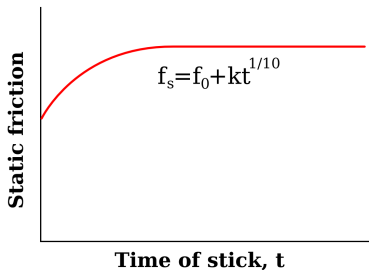
Real friction :: time and velocity

First approximation:

- Friction coefficient does not depend on time

Exceptions:

- creeping materials



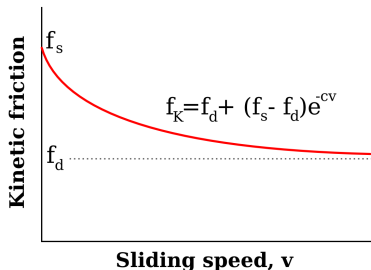
Evolution of the static coefficient of friction with the time of repose

First approximation:

- Friction coefficient does not depend on sliding velocity

Exceptions:

- if material behaves differently at different loading rate, then the friction depends on the sliding velocity



Kinetic friction decreases with increasing sliding velocity

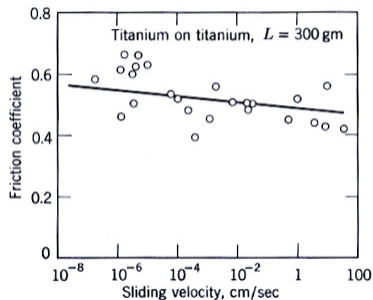
First approximation:

- Friction coefficient does not depend on sliding velocity

Exceptions:

- if material behaves differently at different loading rate (polymers)
- considerable rise in temperature (thermo-mechanical coupling)

Real friction :: velocity



Friction coefficient slightly decreases with increasing velocity of sliding, titanium on titanium

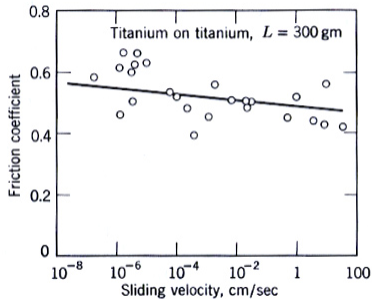
First approximation:

- Friction coefficient does not depend on sliding velocity

Exceptions:

- if material behaves differently at different loading rate (polymers)
- considerable rise in temperature (thermo-mechanical coupling)

Real friction :: velocity



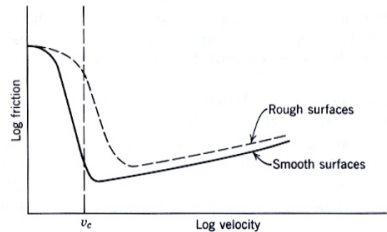
Friction coefficient slightly decreases with increasing velocity of sliding, titanium on titanium

First approximation:

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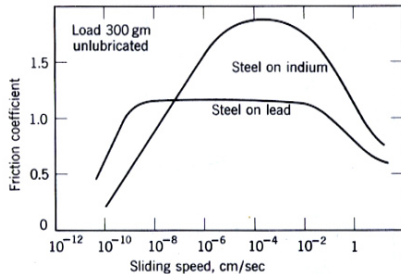
Exceptions:

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- considerable rise in temperature (thermo-mechanical coupling)



Friction coefficient dependence on velocity of sliding for lubricated surfaces

Real friction :: velocity



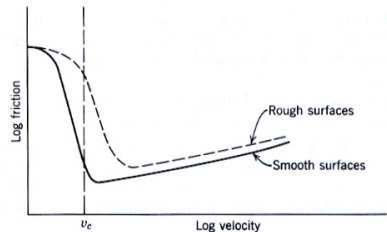
Friction coefficient increases and decreases with increasing velocity of sliding, hard on soft (steel on lead, steel on indium)

First approximation:

- Friction coefficient does not depend on sliding velocity

Exceptions:

- if material behaves differently at different loading rate (polymers)
- considerable rise in temperature (thermo-mechanical coupling)



Friction coefficient dependence on velocity of sliding for lubricated surfaces



Thank you for your attention!
